

From a practical viewpoint, not only are we interested in the work done on an object, but also at the rate at which work is being done on the object.

**POWER** – A measure of the time-rate at which work is done on a system.

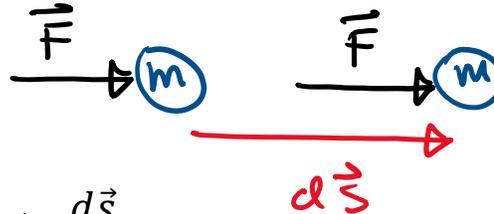
If an amount of work  $W$  is done on an object in a time interval  $t$  by a force  $\mathbf{F}$ , then the average power delivered to the object by the force  $\mathbf{F}$  is given by:

$$\boxed{P_{ave} = \frac{W}{t}} \text{ Average Power}$$

Often the rate at which work is done on an object varies with time and thus we speak about instantaneous power.

$$\boxed{P = \frac{dW}{dt}} \text{ Instantaneous Power}$$

Consider a force  $\mathbf{F}$  acting on a particle over a very small displacement  $d\mathbf{s}$ . The work done by  $\mathbf{F}$  is given by:



$$dW = \vec{F} \cdot d\vec{s}$$

$$P = \frac{dW}{dt} = \frac{\vec{F} \cdot d\vec{s}}{dt} = \vec{F} \cdot \frac{d\vec{s}}{dt}$$

$$\boxed{P = \vec{F} \cdot \vec{v}}$$
 Instantaneous Power (instantaneous rate at which  $\mathbf{F}$  does work on particle)

$$\boxed{P = Fv \cos \theta}$$
 Instantaneous Power

In general power is the time-rate of energy transfer to a system by any method:

$$\boxed{P = \frac{dE}{dt}} \text{ Power}$$

However, for our purpose we will consider work to be the method of energy transfer.

### Units

The SI unit of power is the watt(W)

$$1W=1J/s$$

A common unit of power used in the U.S is the horsepower (hp):

$$1 \text{ hp} = 746 \text{ W} = 0.75 \text{ KW}$$